

**ÇARPARLARA AYIRMA VE ÖZDEŞLİKLER**

$$1. \frac{3x^2y^2 - 3xy^3}{6x^3y - 6x^2y^2} = \frac{3xy^2 \cdot (x-y)}{6x^2y(x-y)} \\ = \frac{\cancel{3}xy^2}{\cancel{6}x^2y} = \frac{y}{2x}$$

**CEVAP: A**

$$4. \frac{x^2 - 9}{(x+3)^2} : \frac{x-3}{x^2 + 3x} = \frac{(x-3).(x+3)}{(x+3).(x+3)} : \frac{x-3}{x.(x+3)} \\ = \frac{(x-3).(x+3)}{(x+3).(x+3)} \cdot \frac{x.(x+3)}{x-3} \\ = x$$

**CEVAP: A**

$$2. \frac{x^2 - x - 20}{x^2 + 2x - 8} : \frac{x+1}{x^2 + 5x} \\ = \frac{x^2 - 25}{x^2 - x - 2} \\ = \frac{\cancel{(x-5)}(x+4) \cdot x(x+5)}{\cancel{(x+4)}(x-2) \cdot \cancel{x+1}} = x \\ = \frac{(x-5)(x+5)}{(x-2)(x+1)}$$

**CEVAP: C**

$$5. \frac{x^2 - 1}{x^2 - 2x - 3} : \frac{1}{x-3} = \frac{(x-1).(x+1)}{(x-3).(x+1)} \cdot (x-3) \\ = x-1$$

**CEVAP: A**

$$3. \frac{1}{a+1} - \frac{1}{a-1} = \frac{\cancel{a}-1-\cancel{a}-1}{(\cancel{a}+1)(\cancel{a}-1)} \\ = \frac{1}{a+1} + \frac{1}{a-1} = \frac{\cancel{a}-1+\cancel{a}+1}{(\cancel{a}+1)(\cancel{a}-1)} \\ = \frac{-2}{2a} \\ = -\frac{1}{a}$$

**CEVAP: E**

$$6. \frac{a^2 - bc - b^2 - ac}{a+b} + b + c = \frac{a^2 - b^2 - bc - ac}{a+b} + b + c \\ = \frac{(a-b)(a+b) - c(a+b)}{a+b} + b + c \\ = \frac{(a-b)(a-b-c)}{a+b} + b + c \\ = a - \cancel{b} - \cancel{c} + \cancel{b} + \cancel{c} \\ = a$$

**CEVAP: A**



7. 
$$\frac{\frac{x^3+1}{1} - \frac{1}{x} - \frac{1}{x^2}}{(x)} : \frac{x^2}{x+1}$$
  

$$= \frac{(x+1)(x^2-x+1)}{x-1-x^2} \cdot \frac{x+1}{x^2}$$

$$= \frac{(x+1)(x^2-x+1)}{-x^2+x-1} \cdot \frac{x+1}{x^2}$$

$$= \frac{x^2 \cdot (x+1) \cdot (x^2-x+1) \cdot (x+1)}{-(x^2-x+1) \cdot x^2}$$

$$= -(x+1)^2 = -x^2 - 2x - 1$$

**CEVAP: C**

8. 
$$\frac{a^3b-b}{a^2-1} : \frac{a^2b+a \cdot b+b}{a^2+a}$$
  

$$= \frac{b(a^3-1)}{(a-1)(a+1)} : \frac{b(a^2+a+1)}{a(a+1)}$$
  

$$= \frac{b'(a-1)(a^2+a+1)}{(a-1)(a+1)} \cdot \frac{a \cdot (a+1)}{b'(a^2+a+1)}$$
  

$$= a$$

**CEVAP: A**

9. 
$$\frac{\frac{x^3-1}{x-1} \cdot \frac{x^3+x^2+x}{x^2}}{(x-1)} \cdot \frac{x^2}{x(x^2+x+1)}$$
  

$$= \frac{x^2}{x} = x$$

**CEVAP: E**

10. 
$$\frac{x+1-\frac{3}{x-1}}{x+2-\frac{4}{x-1}} = \frac{(x-1).(x+1)-3}{(x+2).(x-1)-4}$$
  

$$= \frac{x^2-1-3}{x^2+x-2-4}$$
  

$$= \frac{x^2-4}{x^2+x-6}$$
  

$$= \frac{x-1}{x-1}$$
  

$$= \frac{(x-2).(x+2)}{(x+3)(x-2)}$$
  

$$= \frac{x-1}{x-1}$$
  

$$= \frac{(x-2).(x+2)}{(x+3).(x-2)}$$
  

$$= \frac{x+2}{x+3}$$

**CEVAP: C**



**ÇARPARLARA AYIRMA VE ÖZDEŞLİKLER**

11.

$$\frac{\frac{x^2}{4} - \frac{1}{9}}{\frac{x}{2} + \frac{1}{3}} = \frac{1}{9}$$

$$\left(\frac{x}{2}\right)^2 - \left(\frac{1}{3}\right)^2 = \frac{1}{9}$$

$$\frac{x}{2} + \frac{1}{3} = \frac{9}{9}$$

$$\left(\frac{x}{2} - \frac{1}{3}\right)\left(\frac{x}{2} + \frac{1}{3}\right) = \frac{1}{9}$$

$$\frac{x}{2} + \cancel{\frac{1}{3}} = \cancel{\frac{1}{9}}$$

$$\frac{x}{2} - \frac{1}{3} = \frac{1}{9} \quad \text{ise} \quad \frac{x}{2} = \frac{1}{9} + \frac{1}{3}$$

$$\frac{x}{2} = \frac{4}{9} \quad \text{buradan} \quad x = \frac{8}{9} \quad \text{dur.}$$

**CEVAP: C**

13.

$$\frac{5x^3y - 40x^2y + 80xy}{4x^3y - 64xy}$$

$$= \frac{5xy(x^2 - 8x + 16)}{4xy(x^2 - 16)}$$

$$= \frac{5 \cdot (x-4)^2}{4 \cdot (x^2 - 4^2)} = \frac{5 \cdot (x-4)(x-4)}{4(x-4)(x+4)}$$

$$= \frac{5 \cdot (x-4)}{4(x+4)}$$

**CEVAP: C**

14.

$$\left( \frac{x^3 + 1}{x+1} : \frac{x^2 - x + 1}{x-1} \right) \cdot \frac{1}{x-1}$$

$$= \frac{(x+1) \cdot (x^2 - x + 1)}{x+1} \cdot \frac{x-1}{x^2 - x + 1} \cdot \frac{1}{x-1}$$

$$= 1$$

**CEVAP: E**

12.

$$\left[ \frac{a^2 + ab + b^2}{4a^2 - 1} \right]^{-1} \cdot \frac{a^3 - b^3}{4a^2 - 4a + 1} : (a - b)$$

$$= \frac{(2a)^2 - 1^2}{a^2 + ab + b^2} \cdot \frac{(a-b)(a^2 + ab + b^2)}{(2a-1)^2} \cdot \frac{1}{a-b}$$

$$= \frac{(2a-1)(2a+1)}{(2a-1)^2} = \frac{2a+1}{2a-1}$$

**CEVAP: C**

15.

$$\frac{\frac{x-4}{x} + 3}{\frac{x+8}{x} + 6} : \frac{x-1}{x^2 - 4} = \frac{\frac{x^2 - 4 + 3x}{x}}{\frac{x^2 + 8 + 6x}{x}} : \frac{x-1}{(x-2)(x+2)}$$

$$= \frac{\frac{x^2 + 3x - 4}{x}}{\frac{x^2 + 6x + 8}{x}} \cdot \frac{(x-2)(x+2)}{x-1}$$

$$= \frac{(x+4)(x-1)}{(x+2)(x+4)} \cdot \frac{x}{(x+2)(x+4)} \cdot \frac{(x+2)(x-2)}{x-1}$$

$$= x-2$$

**CEVAP: D**

16.  $4x^2 + 20x + k$  ifadesi bir tam kare ise

$$4x^2 + 20x + k = (2x + 5)^2$$

$$4x^2 + 20x + k = 4x^2 + 20x + 25$$

$$k = 25$$

**CEVAP: E**

17.  $\frac{x-5}{x^2-4x+3} = \frac{M}{x-3} + \frac{N}{x-1}$

$$\frac{x-5}{x^2-4x+3} = \frac{Mx - M + Nx - 3N}{x^2 - 4x + 3}$$

$$x-5 = Mx + Nx - M - 3N$$

$$x-5 = (M+N)x - M - 3N$$

$$\begin{array}{r} M+N=1 \\ + -M-3N=-5 \\ \hline -2N=-4 \\ N=2 \text{ ve } M=-1 \end{array}$$

$$M - N = -1 - 2$$

$$= -3$$

**CEVAP: C**

18.  $\frac{x^2 + ax + 6}{x - 1}$  ifadesi sedeleşebiliyor ise  $x^2 + ax + 6$  ifadesinin çarpanlarından biri  $x - 1$  dir.

$$x - 1 = 0 \Rightarrow x = 1 \text{ için}$$

$$x^2 + ax + 6 = 0 \text{ olmalıdır.}$$

$$1^2 + a \cdot 1 + 6 = 0$$

$$7 + a = 0$$

$$a = -7$$

**CEVAP: B**

19.  $\frac{x^2 + ax - 8}{x^2 - 3x + 2} = \frac{x^2 + ax - 8}{(x-2) \cdot (x-1)}$

ifadesi sadeleşebiliyor ise  $x^2 + ax - 8$  ifadesinin çarpanlarından biri  $x - 2$  veya  $x - 1$  olmalıdır.

$$x - 2 = 0 \Rightarrow x = 2 \quad x - 1 = 0 \Rightarrow x = 1$$

$$\text{für } x^2 + ax - 8 = 0 \quad \text{für } x^2 + ax - 8 = 0$$

olmalıdır. olmalıdır.

$$2^2 + a \cdot 2 - 8 = 0 \quad 1^2 + a \cdot 1 - 8 = 0$$

$$2a = 4 \quad a - 7 = 0$$

$$a = 2 \quad a = 7$$

a'nın alabileceği değerler toplamı

$$2 + 7 = 9$$

**CEVAP: D**

20.  $\frac{x^2 + ax + b}{x^2 - 4x + 3}$  ifadesinin sadeleştirilmiş biçimi

$$\text{çimi } \frac{x+4}{x-1} \text{ olduğuna göre,}$$

$$\frac{x^2 + ax + b}{x^2 - 4x + 3} = \frac{x+4}{x-1} \text{ olmalıdır.}$$

$$\frac{x^2 + ax + b}{(x-3)(x-1)} = \frac{x+4}{x-1}$$

$$x^2 + ax + b = (x-3)(x+4)$$

$$x^2 + \underline{ax+b} = \underline{x^2+x-12}$$

$$a = 1 \text{ ve } b = -12$$

$$a + b = 1 - 12$$

$$= -11$$

**CEVAP: A**